



# Green Ridge Primary Academy Maths Mastery

**REACH2**  
ACADEMY TRUST

  
GREEN RIDGE  
PRIMARY ACADEMY

# What is Maths Mastery?

- Maths mastery is a teaching and learning approach that aims for pupils to develop deep understanding of maths rather than being able to memorise key procedures or resort to rote learning.
- The end goal and expectation is for all pupils (with very limited exceptions) to have acquired the fundamental facts and concepts of maths for their year or key stage such that by the end of it they have achieved mastery in the maths they have been taught. At this point they are ready to move confidently on to their next stage of maths.

# Maths Mastery

- Developing a deep understanding of maths requires careful and systematic progress through various stages within each mathematical topic.
- These are:
  - Concrete – using physical resources to help ‘feel’ the maths.
  - Pictorial – using pictures, diagrams or other representations to ‘see’ the maths.
  - Abstract – using the numerals and written methods to complete maths problems and calculations.



# Concrete resources

- Resources we use include:



Numicon



Base 10



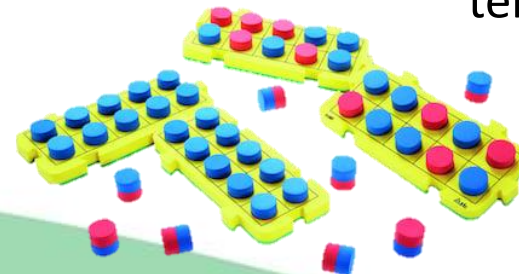
counters



place value counters

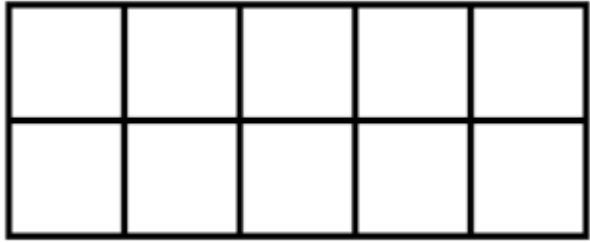


cubes

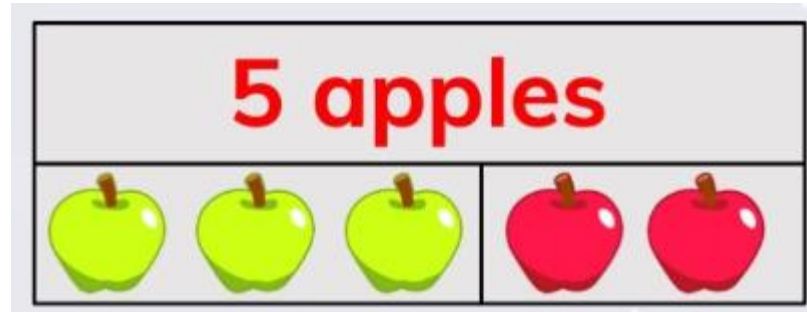


tens frames

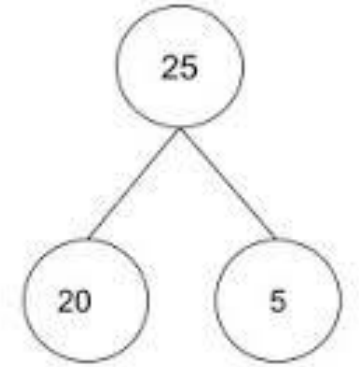
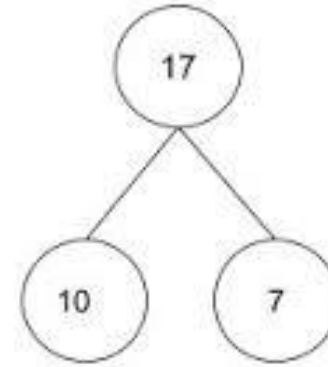
# Pictorial resources



tens frames



bar models



Part-whole models

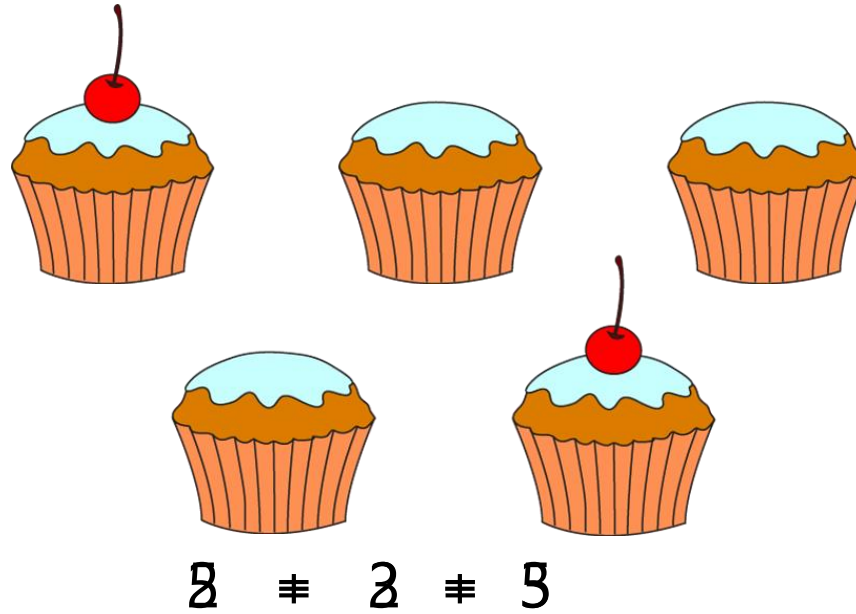
# Number and place value

- Understanding of number and place value is vital for an understanding of maths.
- First steps include counting, 1-to-1 correspondence with counting physical objects, recognising more/less.
- Composition of number is important – 5 is made of 4 and 1, 2 and 3
- This moves on to recognising the numeral and matching this to the number of objects counted (up to 10)
- 10 and beyond introduces a new layer of place value understanding, place value columns can be introduced.
- Identifying that 10 ones make 1 ten, 10 tens make 1 hundred, etc.

# Addition

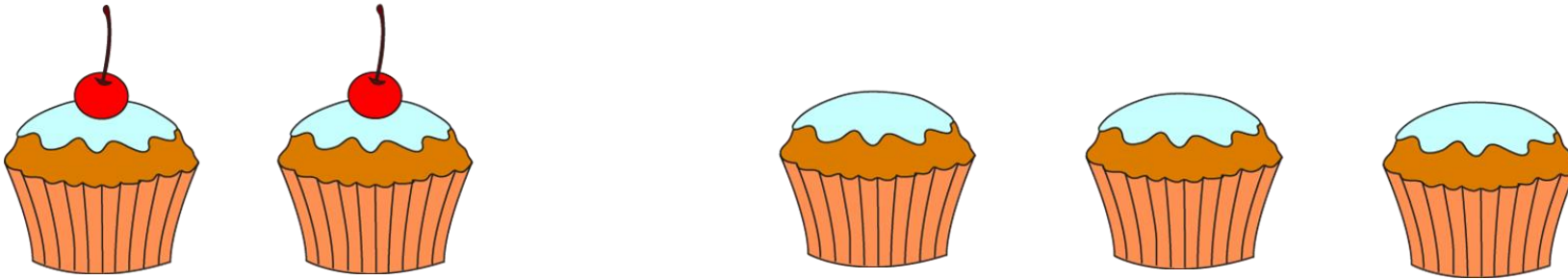
- Combining 2 or more parts to make a whole – starting with physical objects like cubes.
- Use of = to show equivalence between the parts and the whole,
- Partitioning – breaking numbers into their parts to allow them to be added more easily.
  - Bridging 10
  - Adding numbers larger than 10
- Finding missing parts
- Commutative

- 1.5 Aggregation and partitioning – step 2:1





- 1.5 Aggregation and partitioning – step 2:1



$$5 = 3 + 2$$

- 1.5 Aggregation and partitioning – step 2:1

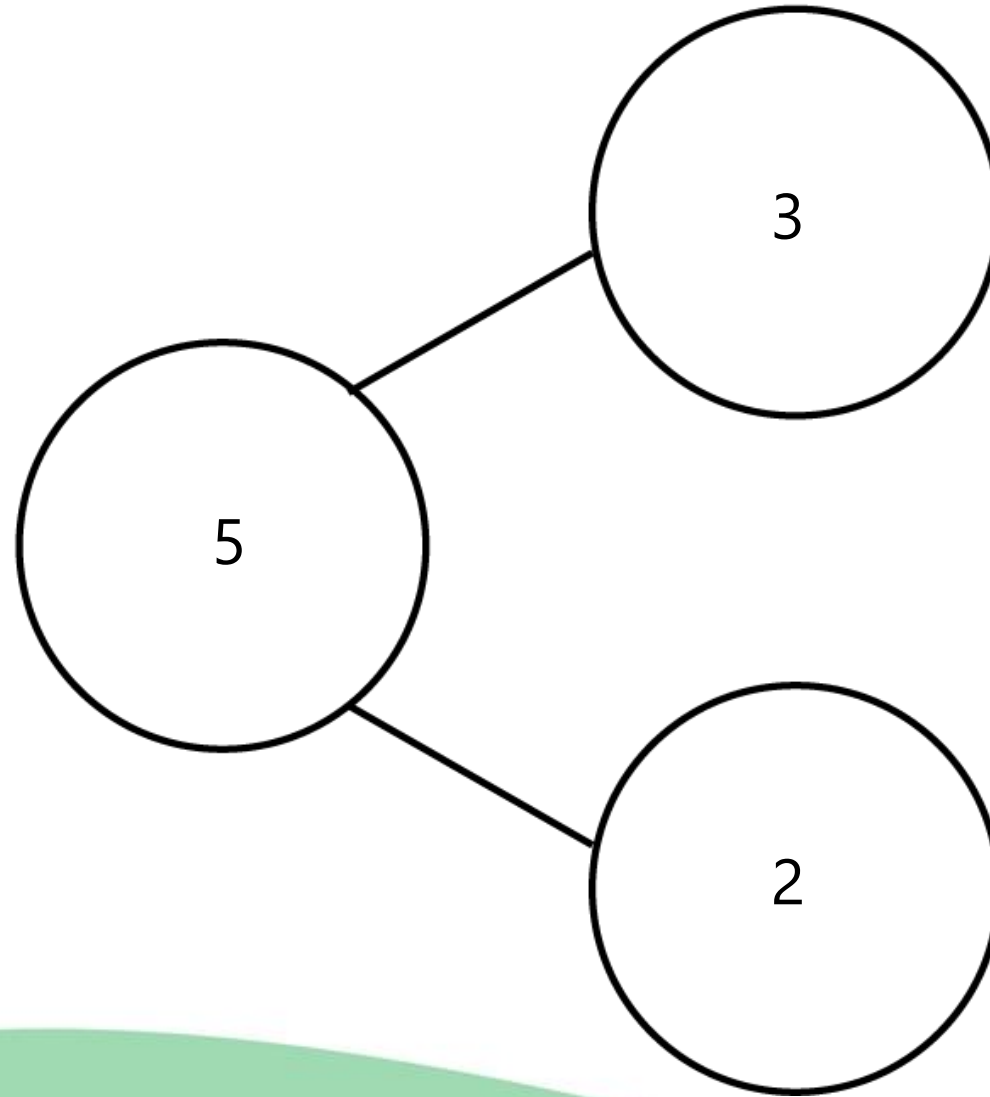
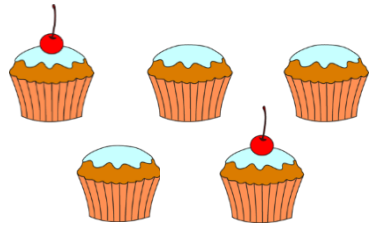
$$2 + 3 = 5$$

$$5 = 2 + 3$$

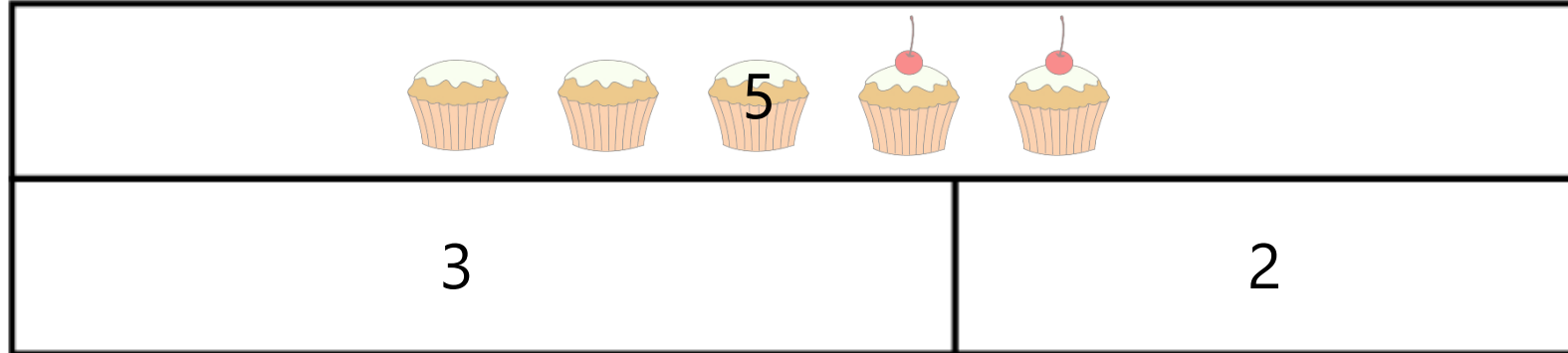
$$3 + 2 = 5$$

$$5 = 3 + 2$$

- 1.5 Aggregation and partitioning – step 2:2



- 1.5 Aggregation and partitioning – step 2:2

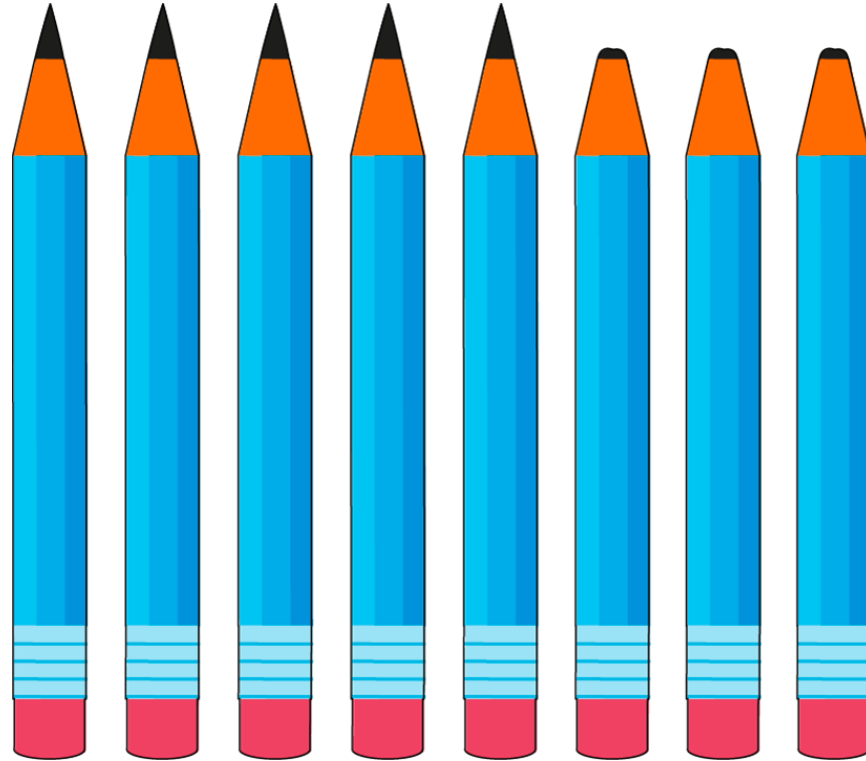




# Subtraction

- Follows the same structure as addition:
- Taking from a whole – using physical objects like cubes.
- Use of  $-$  and  $=$  to show equivalence between the parts and the whole
- Partitioning – using part-whole or bar models
  - Bridging 10
- Finding missing parts

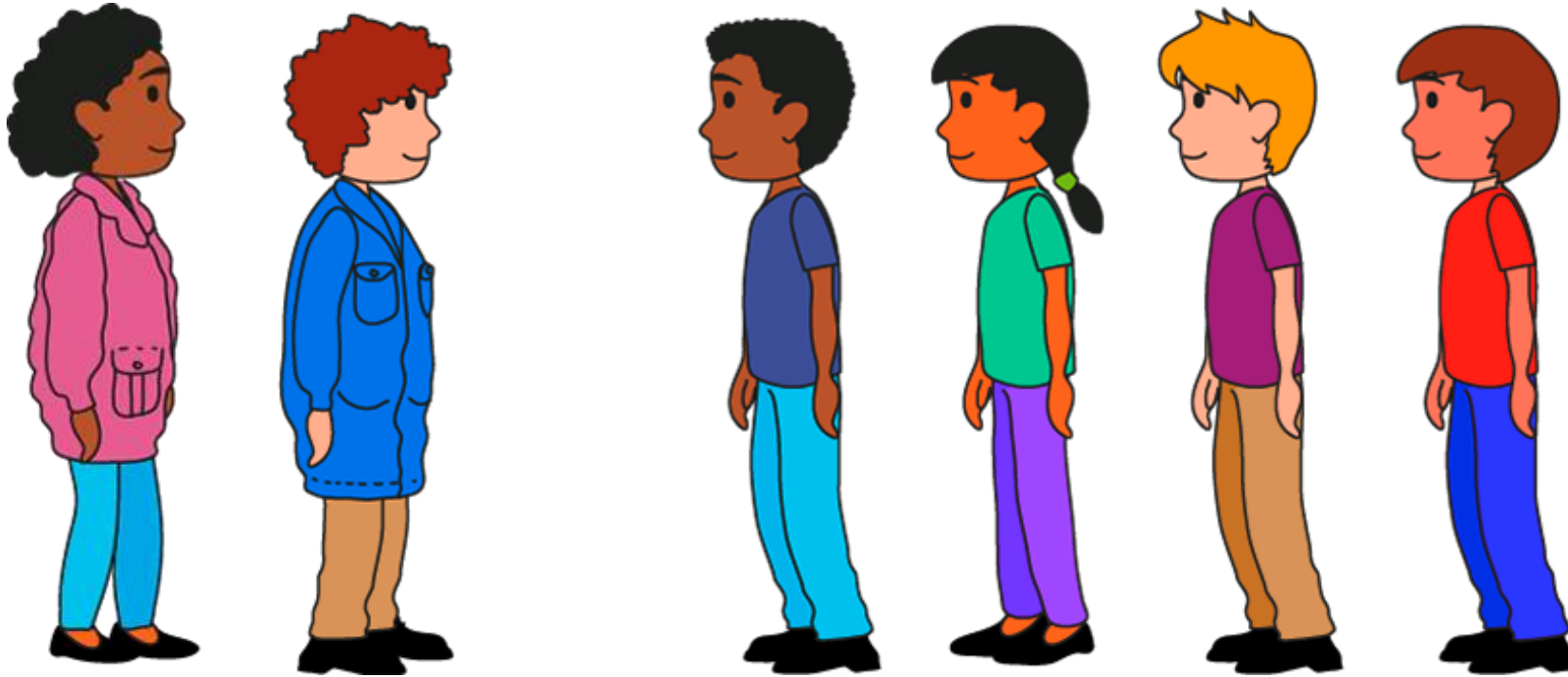
- 1.5 Aggregation and partitioning – step 4:1



5

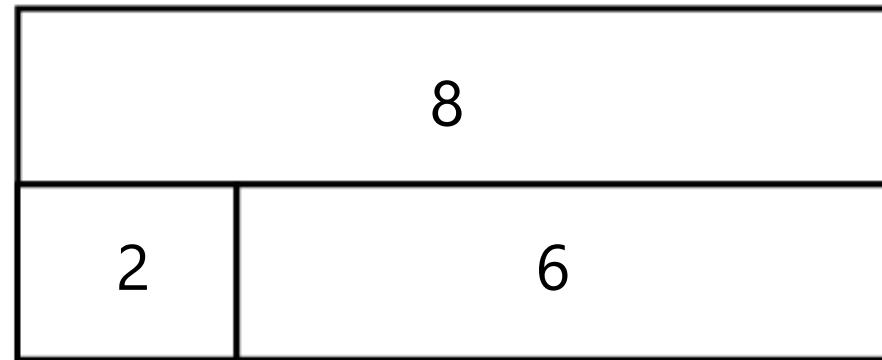
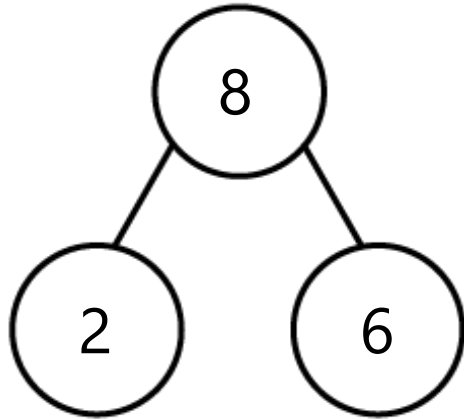
3

- 1.5 Aggregation and partitioning – step 4:2



$$6 - 2 = 4$$

- 1.5 Aggregation and partitioning – step 4:2



$$8 - 2 = 6$$



- 1.5 Aggregation and partitioning – step 4:2



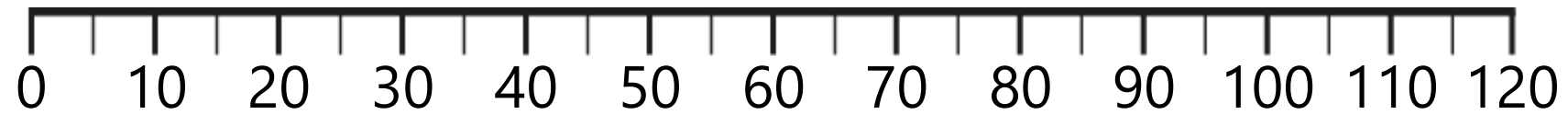
Subtraction

# Multiplication

- Multiplication begins in Year 1 with being able to count in 2s. This is important when starting to understand coins have different values – 2p is worth two 1p coins.
- Developing an understanding of what is the same and what is different – multiplication is groups of the same size.
- Using equipment to make equal groups of focus times table. Counting in groups of ... (unitising).
- Repeated addition

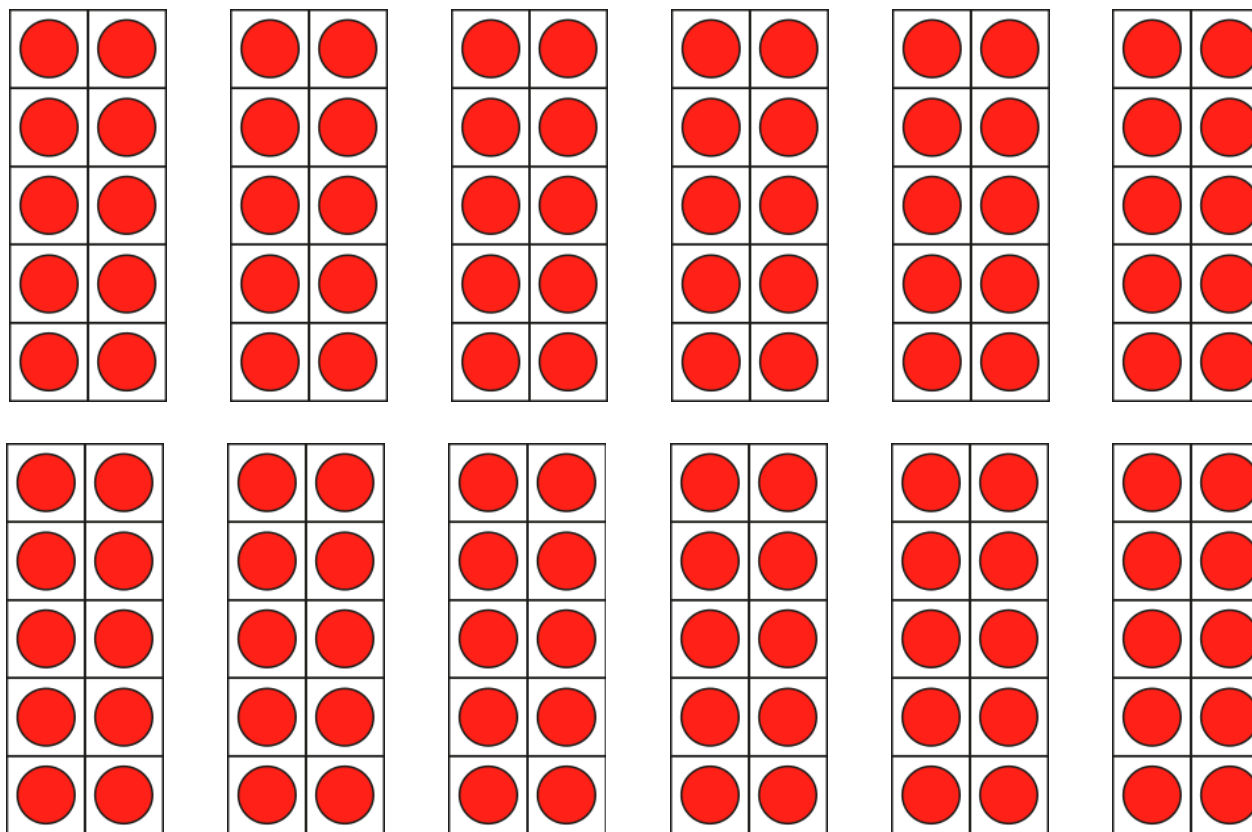
# Multiplication focus

- Year 2 – 2, 5, 10 times tables, doubling and halving.
- Year 3 – 2, 4, 8 (relationship between them), 3, 6, 9 (relationship), 7
- Year 4 – 11 and 12. Consolidation of all tables, MTC at the end of the year
- Year 5 and 6 – application of times tables, starting to use formal written methods.



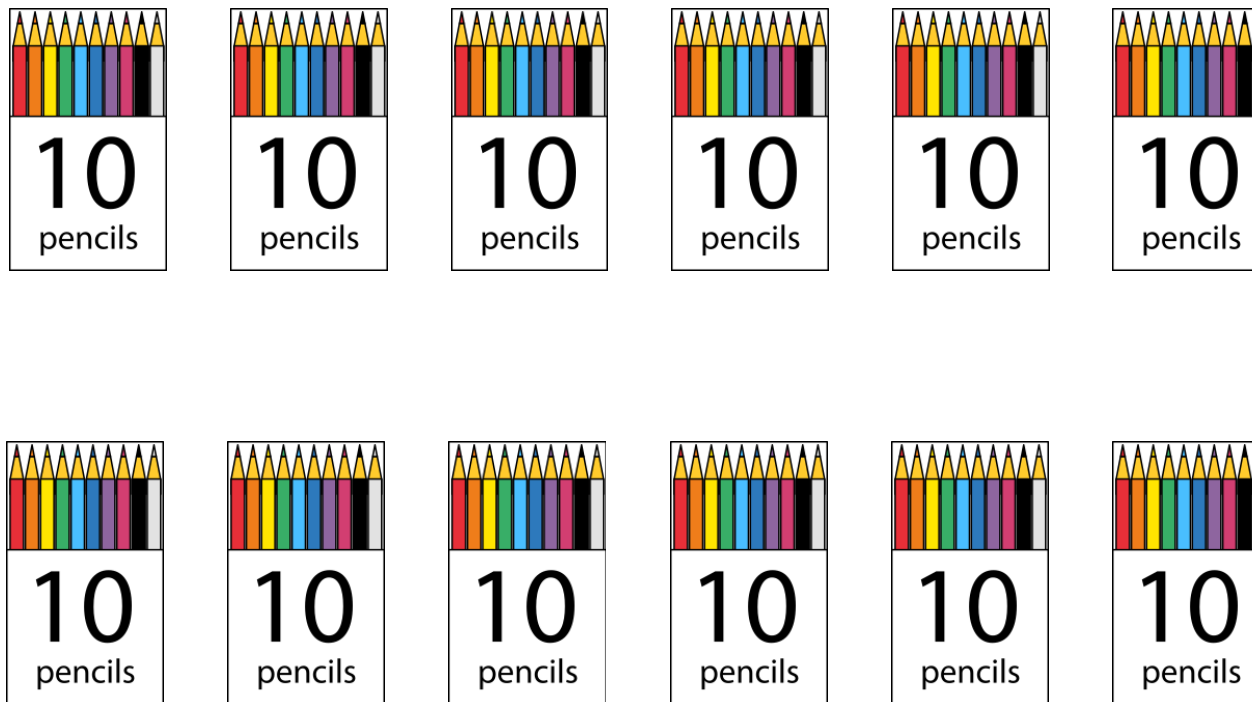


1000	2000	3000	4000	5000	6000	7000	8000	9000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9



~~100~~

~~one hundred~~ ~~thirty~~ ~~and~~ ~~twenty~~



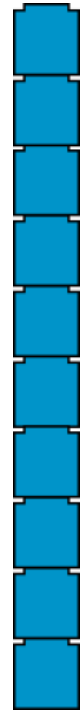
~~100~~

~~one hundred and twenty~~

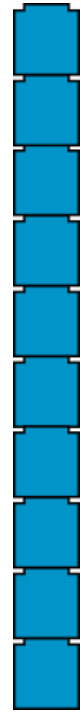


~~100~~

~~one hundred and twenty~~

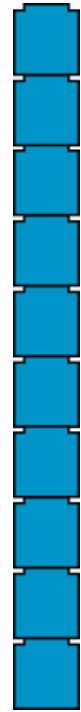


10  
ten



20  
twenty

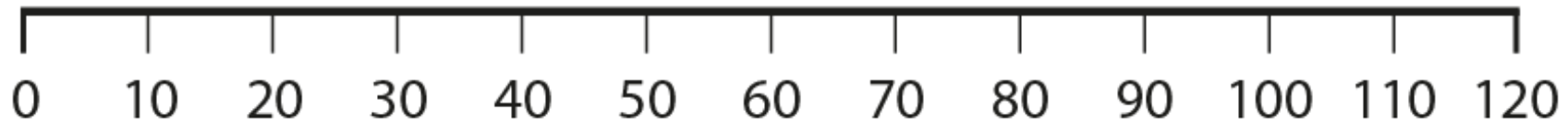
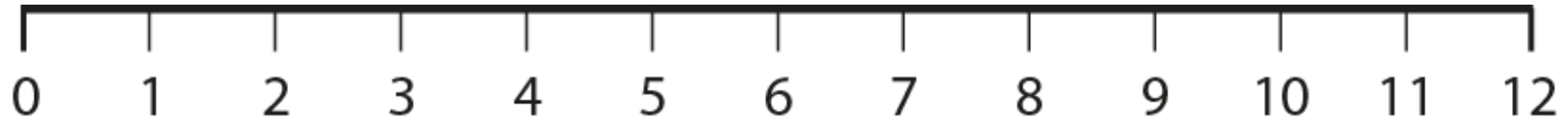
30  
thirty

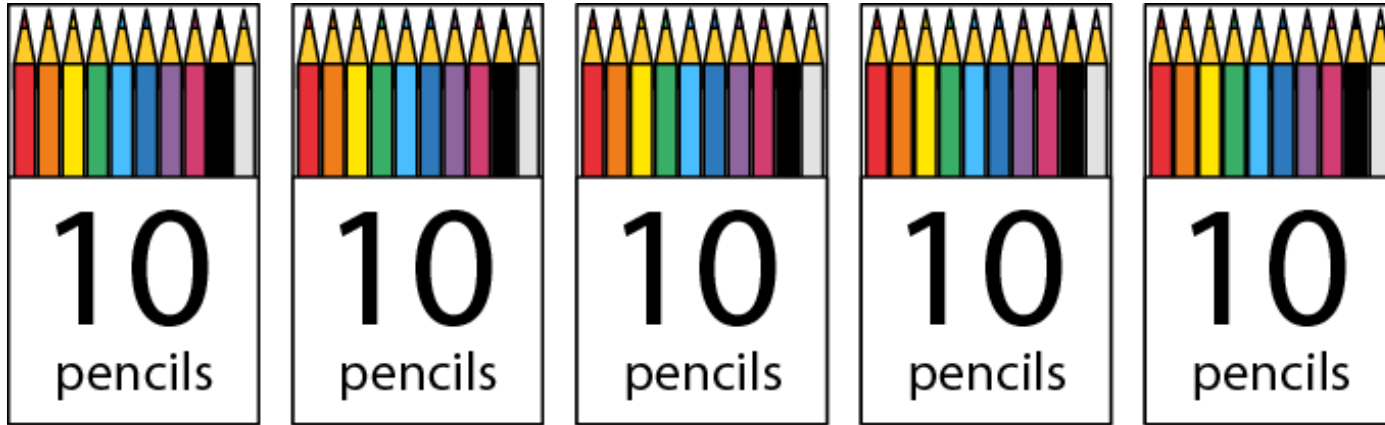


40  
forty



$$4 \times 10 = 40$$



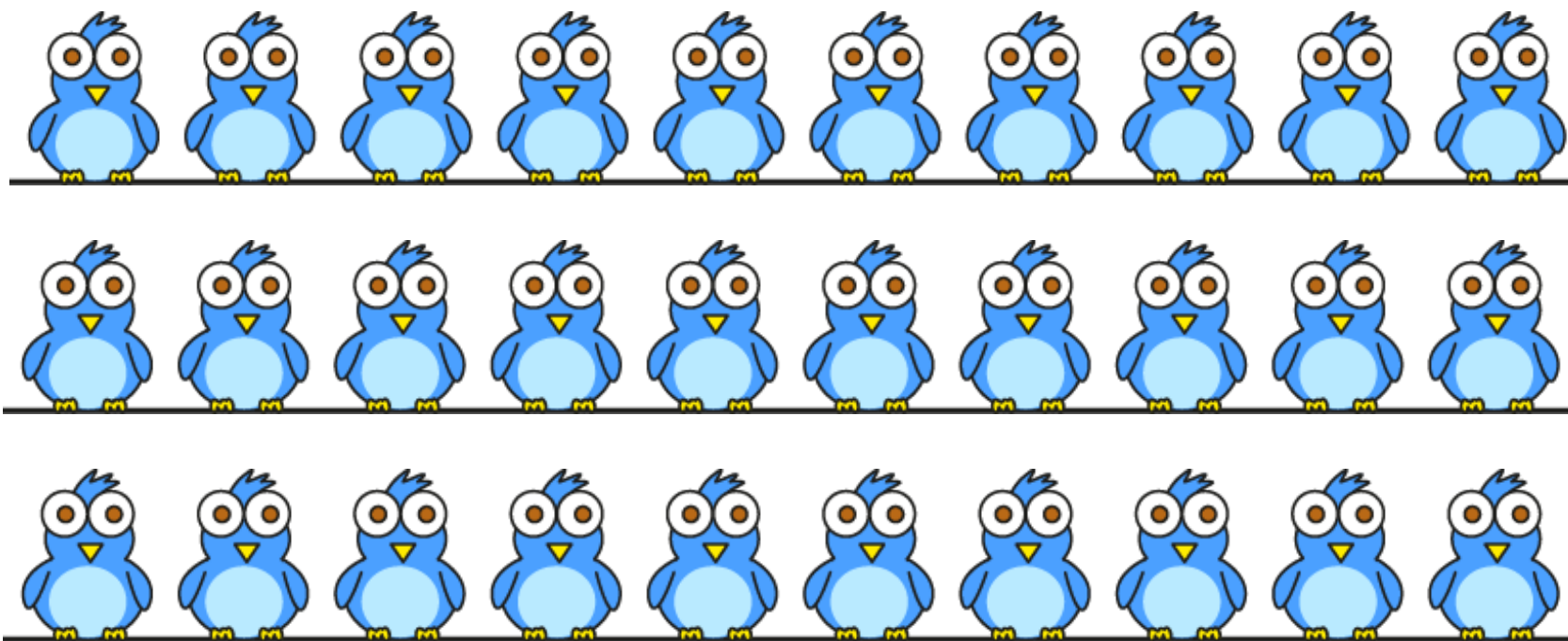


$$\boxed{5} \times 10 = \boxed{50}$$

$$10 \times \boxed{5} = \boxed{50}$$



There are 10 birds on each wire.  
Altogether there are 30 birds. How many wires are there?

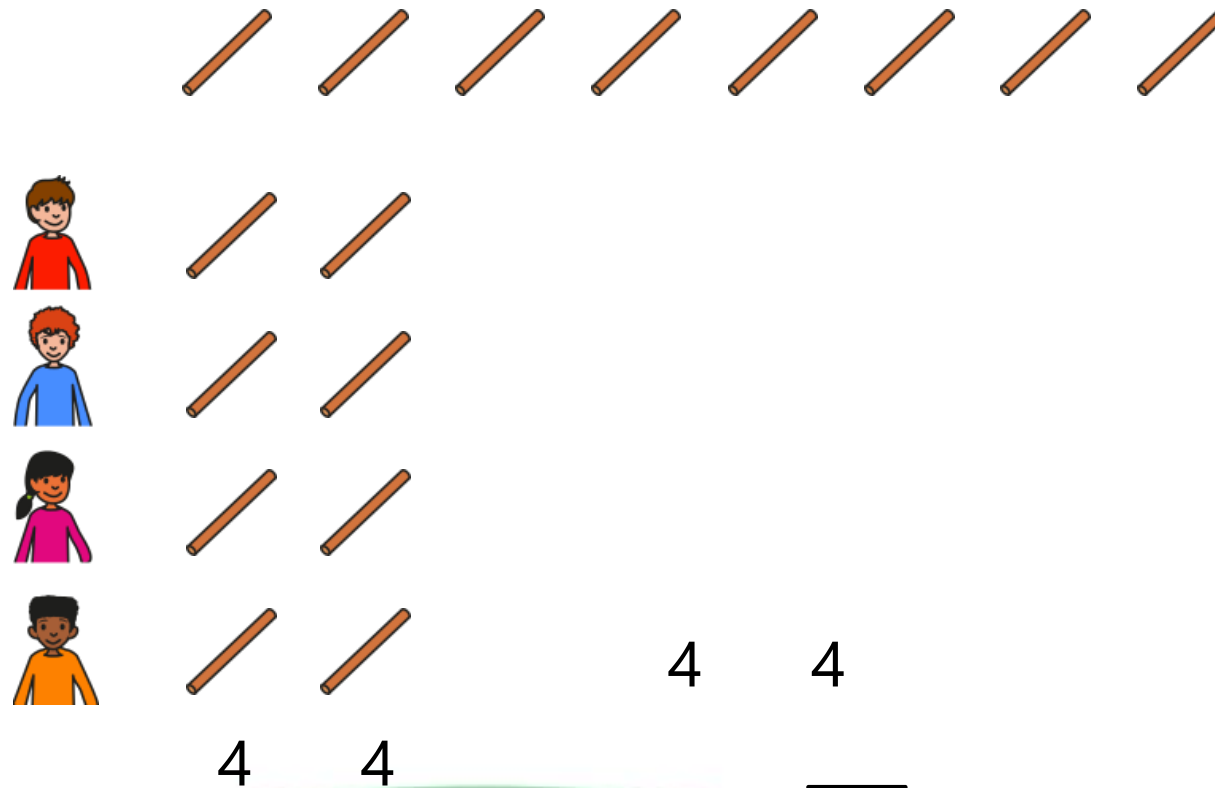


$$\boxed{3} \times 10 = 30$$

# Division

- Division follows Multiplication.
- Division can be **sharing into** and **sharing between**
  - Sharing into groups of 2
  - Sharing between 2 groups
- Division can include a remainder – this is when the groups are made equal, but some pieces cannot be included.
- Dividing practically can lead to and support written methods.
- Understanding of partitioning and place value are incredibly important for division.

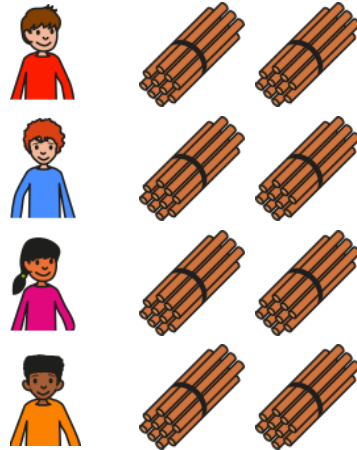
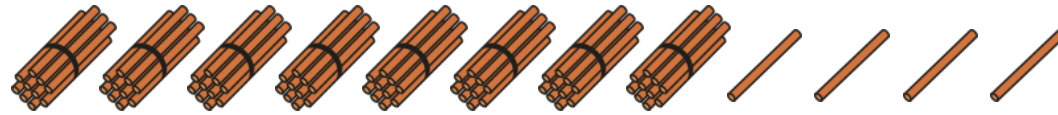
8 sticks shared equally between 4 children.  
How many sticks each?



$$8 \div 4 = \boxed{2}$$

84 sticks shared equally between 4 children. How many sticks each?

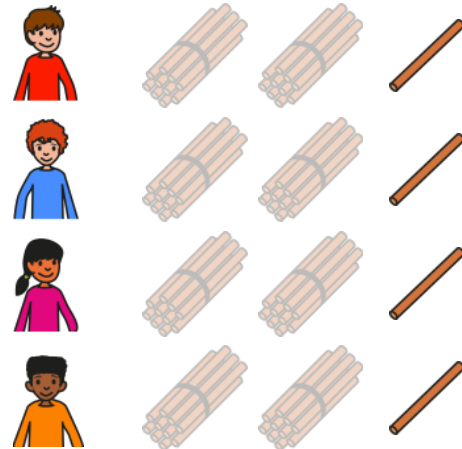
$$84 \div 4 = \square$$



$$8 \text{ tens} \div 4 = 2 \text{ tens}$$

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \square$$

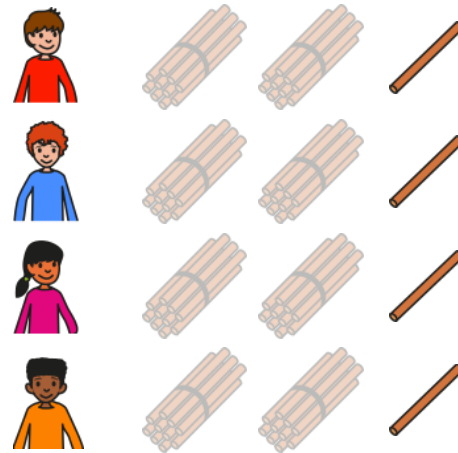


$$8 \text{ tens} \div 4 = 2 \text{ tens}$$

$$4 \text{ ones} \div 4 = 1 \text{ one}$$

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \boxed{21}$$



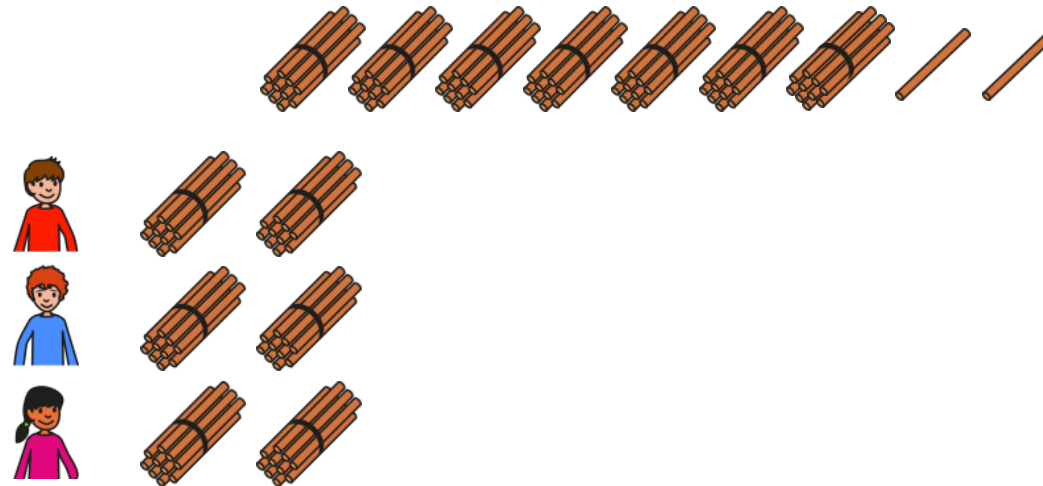
$$8 \text{ tens} \div 4 = 2 \text{ tens}$$

$$4 \text{ ones} \div 4 = 1 \text{ one}$$

$$84 \div 4 = 21$$

72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \square$$

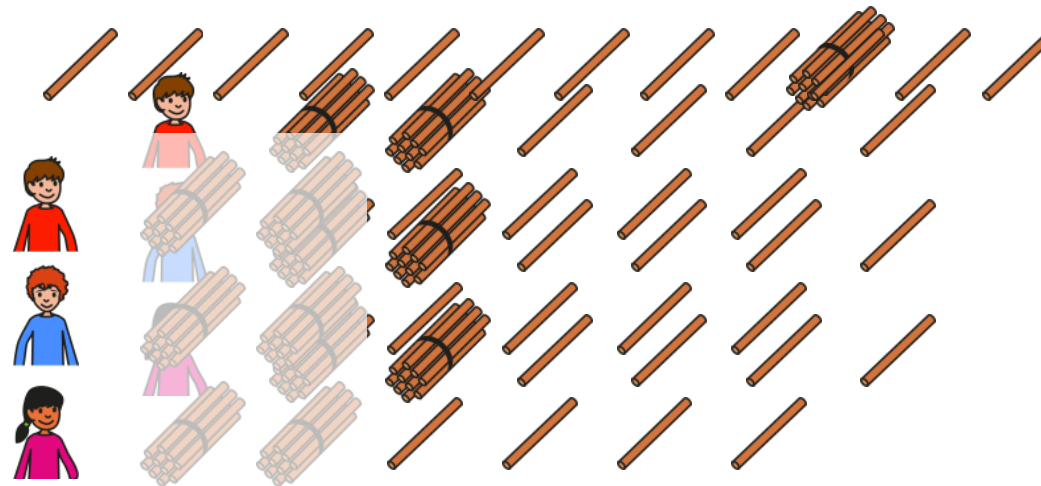


$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$



72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \square$$

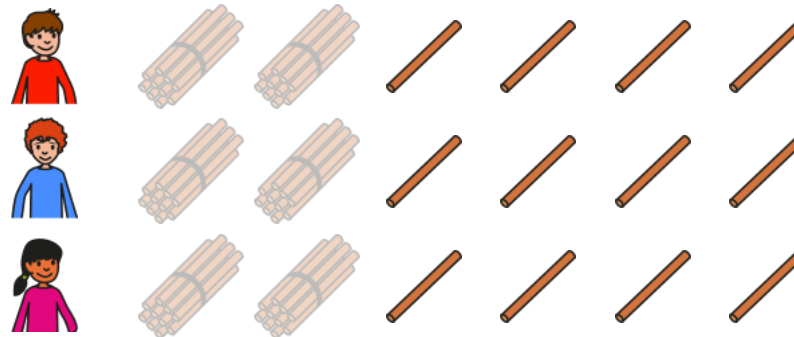


$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

$$12 \text{ ones} \div 3 = 4 \text{ ones}$$

72 sticks shared equally between 3 children. How many sticks each?

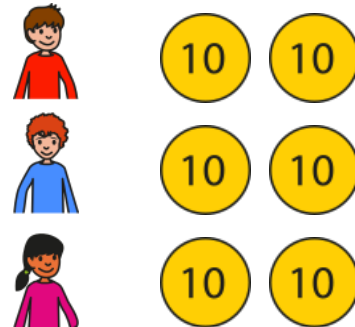
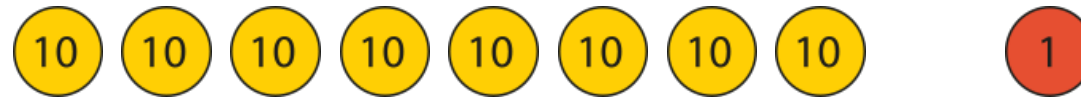
$$72 \div 3 = \boxed{24}$$



6 tens	<del>7</del> tens	$\div 3 = 2$ tens r 1 ten	2 tens
<del>12</del> ones	<del>12</del> ones	$\div 3 = 4$ ones	4 ones
72	$\div$	3	= 24

81 marbles shared equally between 3 children. How many marbles each?

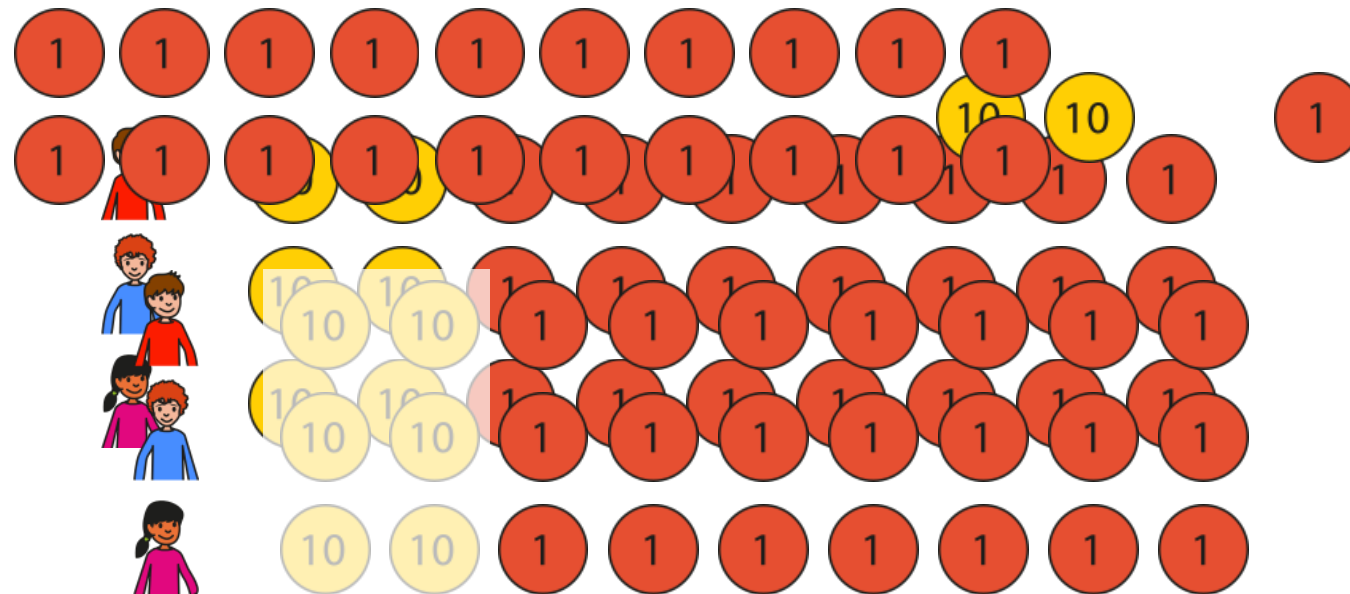
$$81 \div 3 = \square$$



$$8 \text{ tens} \div 3 = 2 \text{ tens r } 2 \text{ tens}$$

81 marbles shared equally between 3 children. How many marbles each?

$$81 \div 3 = \square$$

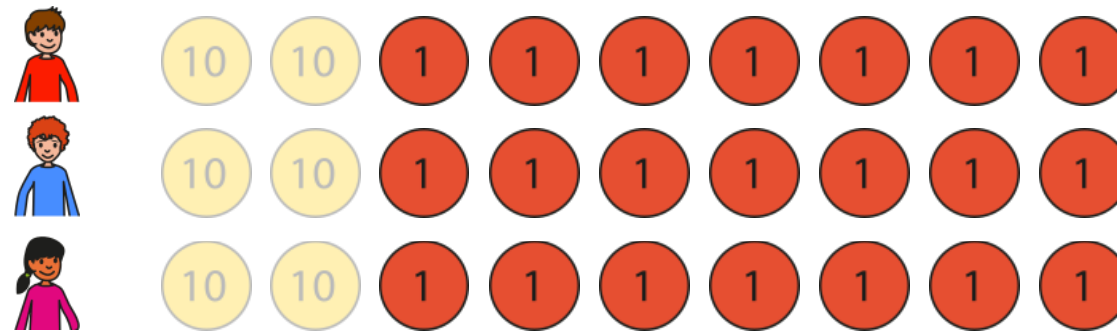


$$8 \text{ tens} \div 3 = 2 \text{ tens r } 2 \text{ tens}$$

$$21 \text{ ones} \div 3 = 7 \text{ ones}$$

81 marbles shared equally between 3 children. How many marbles each?

$$81 \div 3 = \boxed{27}$$

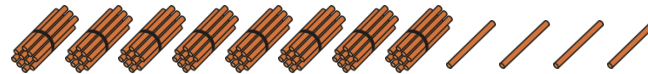


6 tens	<del>8 tens</del>	$\div 3 =$	<del>2 tens</del>	r 2 tens	2 tens
21 ones	<del>21 ones</del>	$\div 3 =$	<del>7 ones</del>	=	7 ones
81	$\div$	3	=		27

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \square$$

Step 1 – write the divisor and dividend:



**10s 1s**

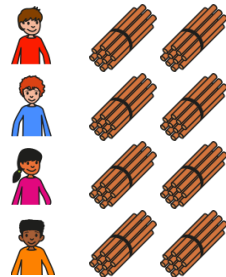
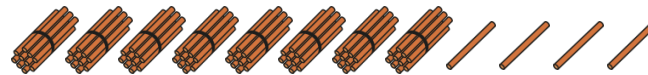
$$4 \overline{) 84}$$

84 divided by 4.

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \square$$

Step 1 – Step 2 the division on the 10s



**10s 1s**

$$8 \text{ tens} \div 4 = 2 \text{ tens}$$

$$\begin{array}{r} 4 \overline{) 84} \end{array}$$

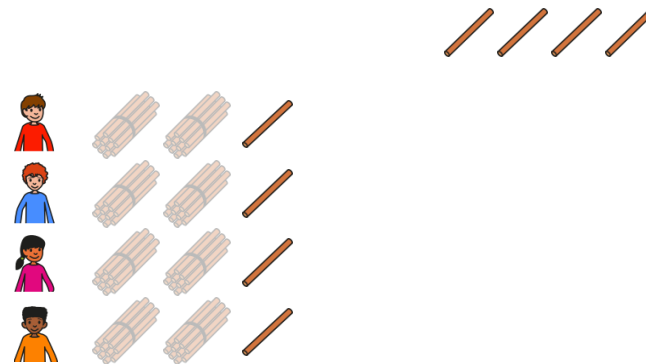
8 tens divided by 4 is equal to 2 tens.



84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \square$$

Step 2—share the 10s:



**10s 1s**

$$\begin{array}{r} 2 \\ 4 \overline{) 84} \end{array}$$

$$8 \text{ tens} \div 4 = 2 \text{ tens}$$

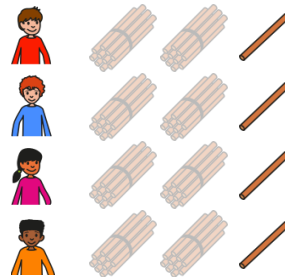
$$4 \text{ ones} \div 4 = 1 \text{ one}$$

8 tens divided by 4 is equal to 2 tens.

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \square$$

Step 3 Summary the 1s:



**10s 1s**

$$\begin{array}{r} 2 \quad 1 \\ 4 \overline{) 84} \end{array}$$

8 tens  $\div$  4 = 2 tens

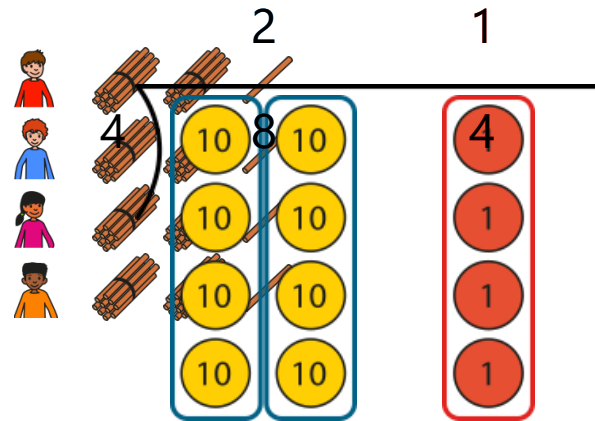
4 ones  $\div$  4 = 1 one

4 ones Each child gets 21 sticks. 1 one.

84 sticks shared equally between 4 children. How many sticks each?

$$84 \div 4 = \boxed{21}$$

Summary  
**10s**      **1s**



$$\begin{array}{r} 21 \\ 4 \overline{) 84} \end{array}$$

8 tens  $\div$  4 = 2 tens

4 ones  $\div$  4 = 1 one

Each child gets 21 sticks.

$84 \div 4 = 21$	$\begin{array}{r} 21 \\ 4 \overline{) 84} \end{array}$
$\text{dividend} \div \text{divisor} = \text{quotient}$	$\begin{array}{r} \text{quotient} \\ \text{divisor} \overline{) \text{dividend}} \end{array}$

72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \square$$

Step 1 – write the divisor and the dividend:

$$3 \overline{) 72}$$

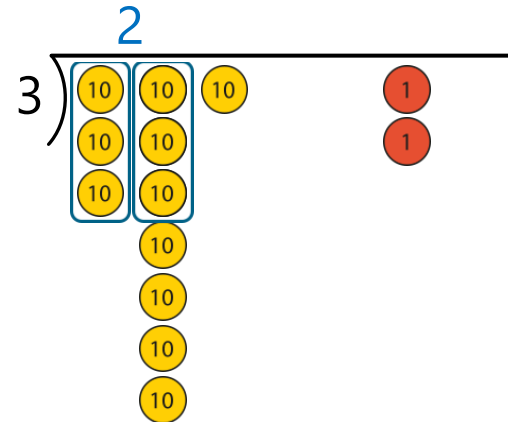


72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \square$$

Step 1 – write the dividend: ~~Step 2 – divide the 10s~~ Use the dividend:

$$3 \overline{) 72}$$



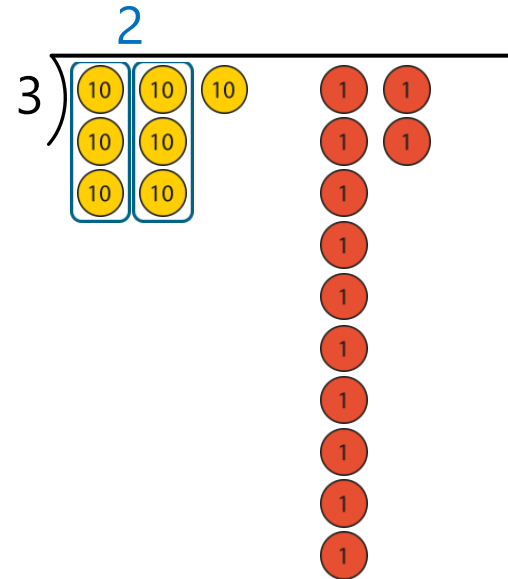
$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \square$$

Step 3 share the 10s:

$$\begin{array}{r} 2 \\ 3 \overline{) 72} \end{array}$$



$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

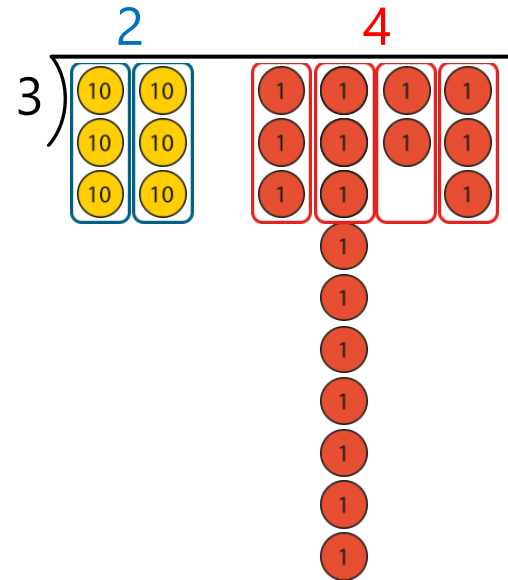


72 sticks shared equally between 3 children. How many sticks each?

$$72 \div 3 = \boxed{24}$$

Step 3 - exchange:

$$\begin{array}{r} 2 \quad 4 \\ 3 \overline{) 7 \quad 12} \end{array}$$



$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

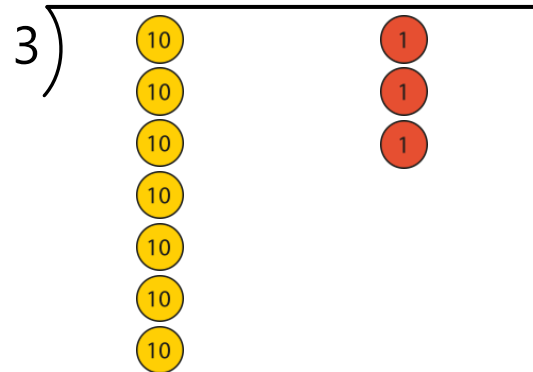
$$12 \text{ ones} \div 3 = 4 \text{ ones}$$

73 sticks shared equally between 3 children. How many sticks each?

$$73 \div 3 = \boxed{\phantom{00}}$$

Step 1 – write the divisor and the dividend:

$$3 \overline{) 73}$$

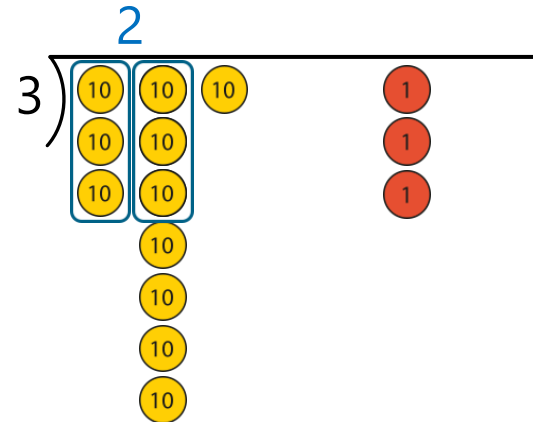


73 sticks shared equally between 3 children. How many sticks each?

$$73 \div 3 = \boxed{\phantom{00}}$$

Step 1 – write the dividend: ~~Step 2 – divide the 10s~~ Use the dividend:

$$3 \overline{) 73}$$



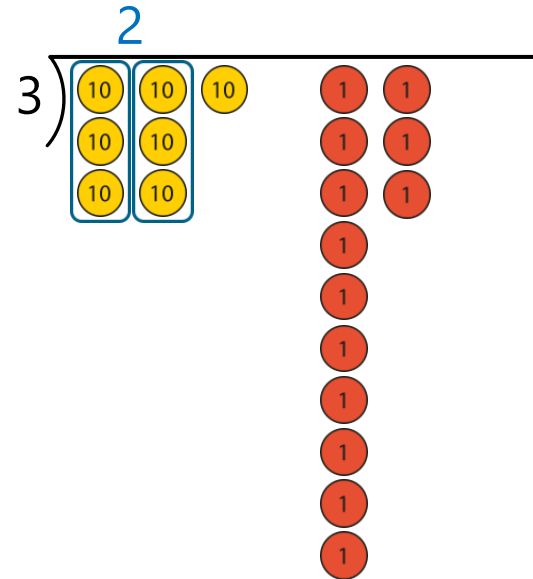
$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

73 sticks shared equally between 3 children. How many sticks each?

$$73 \div 3 = \boxed{\phantom{00}}$$

Step 3 share the 10s:

$$\begin{array}{r} 2 \\ 3 \overline{) 73} \end{array}$$



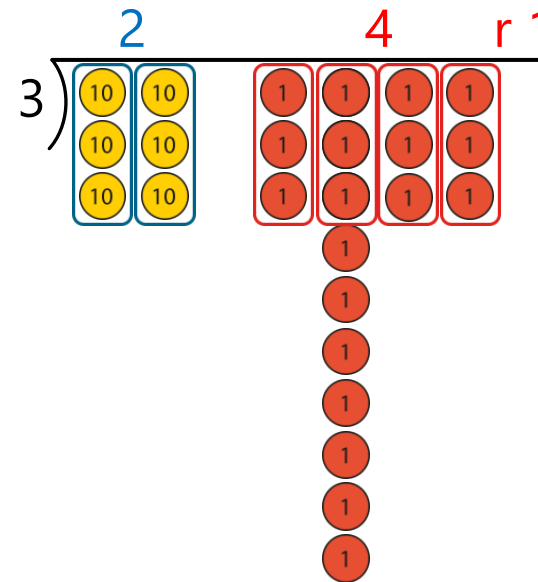
$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

73 sticks shared equally between 3 children. How many sticks each?

$$73 \div 3 = \boxed{24 \text{ r } 1}$$

Step 3 – share the tens:

$$\begin{array}{r} 2 \quad 1 \\ 3 \overline{) 7 \ 3} \end{array}$$



$$7 \text{ tens} \div 3 = 2 \text{ tens r } 1 \text{ ten}$$

$$13 \text{ ones} \div 3 = 4 \text{ ones r } 1 \text{ one}$$

# Fractions

- Importance of fractions being equal parts.
- KS1 – recognise and name common fractions of shapes, objects or quantities.  $\frac{1}{2}$ ,  $\frac{1}{4}$ ,  $\frac{1}{3}$ ,  $\frac{2}{4}$ ,  $\frac{3}{4}$
- KS2:
  - equivalent fractions ( $\frac{2}{4} = \frac{1}{2}$ )
  - Unit and non-unit fractions
  - Adding and subtracting fractions (starting with same denominator)
  - Proper fractions ( $\frac{3}{4}$ ), improper fractions ( $\frac{7}{4}$ ), mixed numbers ( $1\frac{3}{4}$ )
  - Multiplying fractions by whole numbers
  - Multiplying fractions by fractions
  - Dividing fractions by whole numbers

## 3.6 Multiplying whole numbers and fractions Step 1:2



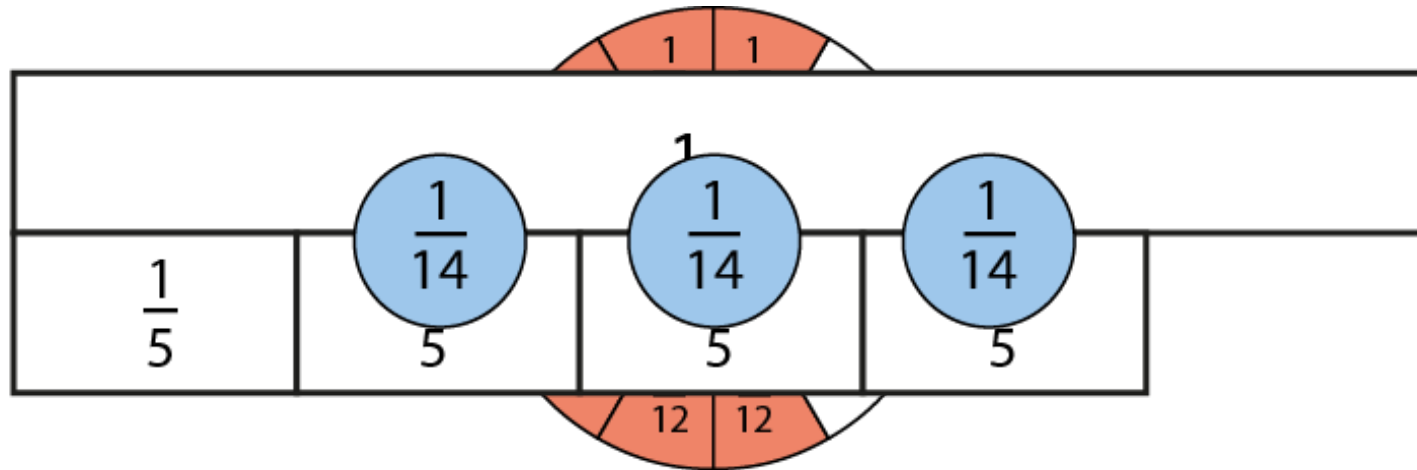
$$\frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

$$4 \times \frac{1}{8}$$

$$\frac{1}{8} \times 4$$

$$\frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} = 4 \times \frac{1}{8} = \frac{1}{8} \times 4$$

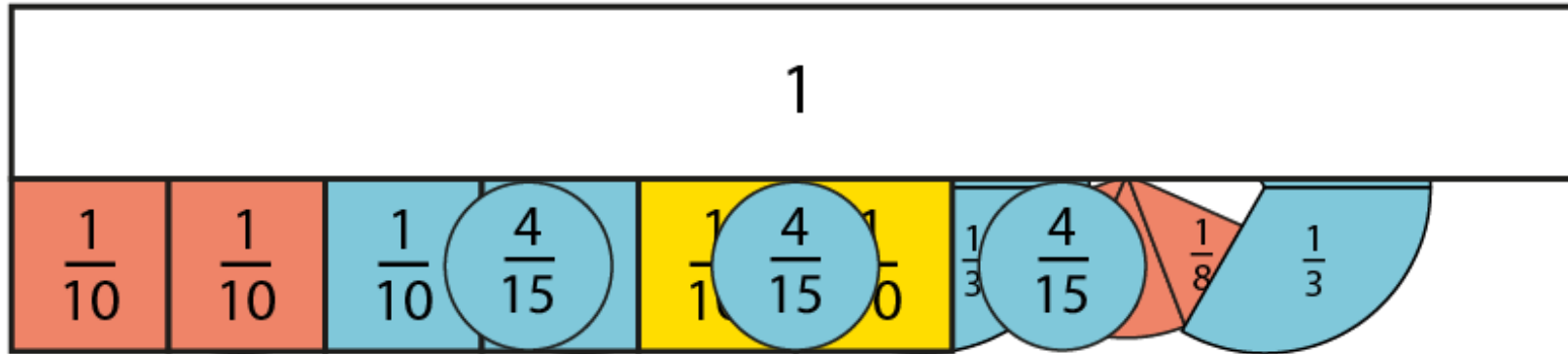
# 3.6 Multiplying whole numbers and fractions Step 1:3



$$\frac{1}{12} + \frac{1}{12} + \frac{1}{12} + \frac{1}{14} + \frac{1}{14} + \frac{1}{14} + \frac{1}{14} + \frac{1}{14} + \frac{1}{14} = \frac{11}{12} + \frac{11}{14} = \frac{11}{12} \times \frac{7}{7} + \frac{11}{14} \times \frac{3}{3} = \frac{77}{84} + \frac{33}{84} = \frac{110}{84} = \frac{55}{42}$$



# 3.6 Multiplying whole numbers and fractions Step 1:6

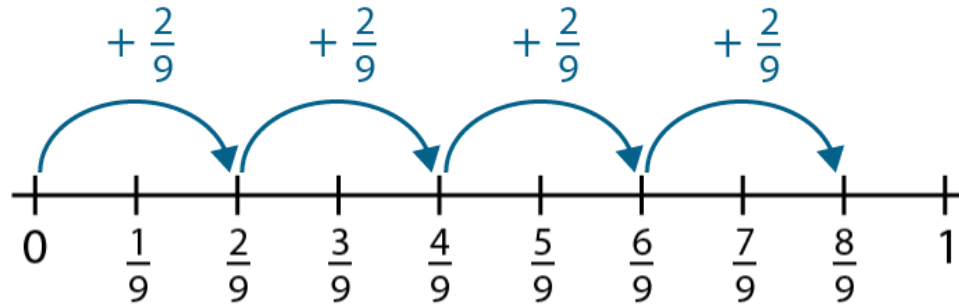
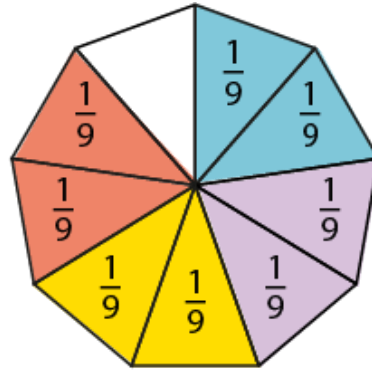


$$\frac{2}{3} + \frac{2}{3} + \frac{2}{3} + \frac{2}{3} + \frac{2}{3}$$

$$3 \times \frac{2}{3}$$

$$\frac{2}{3} \times 3$$

### 3.6 Multiplying whole numbers and fractions Steps 1:8–1:9



$$\frac{2}{9} + \frac{2}{9} + \frac{2}{9} + \frac{2}{9} = \frac{8}{9}$$

$$4 \times \frac{2}{9} = \frac{8}{9}$$

$$\frac{2}{9} \times 4 = \frac{8}{9}$$

# Any Questions?

